

What is claimed is:

1. A method for calculating the financial status of a company, comprising the steps of:
calculating the company's value in accordance with the formula

$$\frac{dV}{V} = (r + \lambda)dt + \sigma dW - dN$$

5 wherein

V is the value of the company,

r is the risk neutral rate,

λ is the intensity of jump arrivals,

σ is the company's volatility,

10 N) is the standard Poisson process,

W is the standard Wiener process,

and t is a time between 0 and T , the maturity of the debt; and

using the company value to calculate a financial metric for the company.

- 15 2. The method of claim 1 wherein the financial metric is the equity value of a company in accordance with the formula

$$S = VN(d_+) - e^{-(r+\lambda)T} DN(d_-) - V(LD/V)^{2(r+\lambda)/\sigma^2+1} N(f_+) + e^{-(r+\lambda)T} D(LD/V)^{2(r+\lambda)/\sigma^2-1} N(f_-);$$

wherein like variables to those defined above define the same values and wherein

$$d_{\pm} = [\ln(S/D) + (r + \lambda \pm \sigma^2/2)T] / \sigma \sqrt{T}$$

$$20 \quad f_{\pm} = [\ln(L^2 D/V) + (r + \lambda \pm \sigma^2/2)T] / \sigma \sqrt{T}$$

D is the value of the debt,

T is the maturity of debt, and

L is relative level at which the company defaults.

- 25 3. The method of claim 1 wherein the financial metric is the debt value of a company in accordance with the formula

$$\delta = VN(d_-) + e^{-(r+\lambda)T} DN(d_-) + V(LD/V)^{2(r+\lambda)/\sigma^2+1} N(f_+) - e^{-(r+\lambda)T} D(LD/V)^{2(r+\lambda)/\sigma^2-1} N(f_-);$$

wherein like variables to those defined above define the same values and wherein

$$d_{\pm} = [\ln(S/D) + (r + \lambda \pm \sigma^2/2)T] / \sigma \sqrt{T}$$

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$$f_{\pm} = [\ln(L^2 D / V) + (r + \lambda \pm \sigma^2 / 2)T] / \sigma \sqrt{T}$$

D is the value of the debt,

T is the maturity of debt, and

L is relative level at which the company defaults.

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4. The method of claim 1 wherein the financial metric is the survival probability of a company in accordance with the formula

$$Q(t) = e^{-\lambda t} \left[N(g_+) - (LD / V)^{2r / \sigma^2} N(g_-) \right] \quad t < T$$

wherein like variables to those defined above define the same values and wherein

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$$g_{\pm} = [\pm \ln(V / LD) + (r + \lambda - \sigma^2 / 2)t] / \sigma \sqrt{t}$$

D is the value of the debt,

T is the maturity of debt,

L is relative level at which the company defaults.

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5. A method in accordance with claim 1 and further comprising the step of calculating the credit default spread (CDS(t)) for very short maturities of the company in accordance with the formula

$$CDS(t) \rightarrow \lambda(1 - R) \text{ when } t \rightarrow 0,$$

wherein R is a recovery level for a selected debt seniority.

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6. A system for calculating the financial status of a company, comprising:

a processor;

a memory connected to the processor and storing instructions for controlling the operation of the processor;

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the processor operative with the instructions in the memory to perform the steps of calculating the company's value in accordance with the formula

$$\frac{dV}{V} = (r + \lambda)dt + \sigma dW - dN$$

wherein

V is the value of the company,

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r is the risk neutral rate,

λ is the intensity of jump arrivals,

σ is the company's volatility,
 N is the standard Poisson process,
 W is the standard Wiener process,
and t is a time between 0 and T , the maturity of the debt; and

5 using the company value to calculate a financial metric for the company.

7. The system of claim 6 wherein the financial metric is the equity value of a company in accordance with the formula

$$S = VN(d_+) - e^{-(r+\lambda)T} DN(d_-) - V(LD/V)^{2(r+\lambda)/\sigma^2+1} N(f_+) + e^{-(r+\lambda)T} D(LD/V)^{2(r+\lambda)/\sigma^2-1} N(f_-);$$

10 wherein like variables to those defined above define the same values and wherein

$$d_{\pm} = [\ln(S/D) + (r + \lambda \pm \sigma^2/2)T] / \sigma \sqrt{T}$$

$$f_{\pm} = [\ln(L^2 D/V) + (r + \lambda \pm \sigma^2/2)T] / \sigma \sqrt{T}$$

D is the value of the debt,

T is the maturity of debt, and

15 L is relative level at which the company defaults.

8. The system of claim 6 wherein the financial metric is the debt value of a company in accordance with the formula

$$\delta = VN(d_-) + e^{-(r+\lambda)T} DN(d_-) + V(LD/V)^{2(r+\lambda)/\sigma^2+1} N(f_+) - e^{-(r+\lambda)T} D(LD/V)^{2(r+\lambda)/\sigma^2-1} N(f_-);$$

20 wherein like variables to those defined above define the same values and wherein

$$d_{\pm} = [\ln(S/D) + (r + \lambda \pm \sigma^2/2)T] / \sigma \sqrt{T}$$

$$f_{\pm} = [\ln(L^2 D/V) + (r + \lambda \pm \sigma^2/2)T] / \sigma \sqrt{T}$$

D is the value of the debt,

T is the maturity of debt, and

25 L is relative level at which the company defaults.

9. The system of claim 6 wherein the financial metric is the survival probability of a company in accordance with the formula

$$Q(t) = e^{-\lambda t} \left[N(g_+) - (LD/V)^{2r/\sigma^2} N(g_-) \right] \quad t < T$$

30 wherein like variables to those defined above define the same values and wherein

$$g_{\pm} = \left[\pm \ln(V / LD) + (r + \lambda - \sigma^2 / 2)t \right] / \sigma \sqrt{t}$$

D is the value of the debt,

T is the maturity of debt,

L is relative level at which the company defaults.

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10. A system in accordance with claim 6 and further comprising the step of calculating the credit default spread (CDS(t)) for very short maturities of the company in accordance with the formula

$$CDS(t) \rightarrow \lambda(1 - R) \text{ when } t \rightarrow 0,$$

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wherein R is a recovery level for a selected debt seniority.

11. A system for calculating the financial status of a company, comprising:

means for calculating the company's value in accordance with the formula

$$\frac{dV}{V} = (r + \lambda)dt + \sigma dW - dN$$

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wherein

V is the value of the company,

r is the risk neutral rate,

λ is the intensity of jump arrivals,

σ is the company's volatility,

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N is the standard Poisson process,

W is the standard Wiener process,

and t is a time between 0 and T , the maturity of the debt; and

means for using the company value to calculate a financial metric for the company.

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12. A method of calculating the financial status of a company, comprising the steps of:

determining the company's value in accordance with the formula

$$\frac{dV}{V} = (r - \lambda \kappa)dt + \sigma dW + (e^J - 1)dN$$

wherein

N is the standard Poisson process with intensity λ ,

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J is a normal variable with mean j and standard deviation k ;

W is the standard Wiener process,

V is the value of the company,

r is the risk neutral rate of the company,

σ is the company volatility,

5 λ is the intensity of the jump arrival,

t is calendar time between today and maturity T ; and

determining that the company defaults if at a sequence of discrete observational times

$t_0 = 0(\text{today}), t_1, t_2, \dots, t_N = T(\text{maturity})$ the value of the company $V_n = V(t_n)$ falls below a

corresponding barrier level $B_1, B_2, \dots, B_N = D$, the barrier levels selected to represent different

10 debt amounts which come due at corresponding times $t_0 = 0(\text{today}), t_1, t_2, \dots, t_N = T(\text{maturity})$.

13. The method of claim 12 and further comprising calculating the transitional probability density function (*TPDF*) for the value of the company conditional on no default occurring between time $t = 0$ and an observational time t_x comprising the steps of:

15 selecting a range for the natural logarithm of the value of the company $U = \ln(V)$:

$$U_{\min} < U < U_{\max}$$

where

$$U_{\min} = -nsd \div \sqrt{(\sigma^2 + k^2)T} + \min(r - \lambda\kappa - \sigma^2 / 2, 0)T$$

and

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$$U_{\max} = nsd \div \sqrt{(\sigma^2 + k^2)T} + \max(r - \lambda\kappa - \sigma^2 / 2, 0)T$$

and where nsd is the number of standard deviations used to characterize the extreme values of the natural logarithm of the value of the company;

dividing the range into an equidistant grid $u_0 = U_{\min}, u_1, \dots, u_m, \dots, u_M = U_{\max}$ of M steps,

with each grid step, denoted by h , equal to $h = (U_{\max} - U_{\min}) / M$, with the total number of

25 points in the grid, which is equal to $M+1$, being a power of 2;

defining the integer $\mu = \text{floor}(-U_{\min} / h)$, where $\text{floor}(\cdot)$ is a mathematical function, which for every number defines an integer less than or equal to this number;

constructing the modified grid as: $\tilde{u}_m = (m - \mu)h$, $m = 0, 1, \dots, M$;

30 defining a grid on the line representing the value of the company using the following formula

$$v_m = V_0 \exp(u_m) \quad m = 0, 1, \dots, M$$

where the initial value of the company V_0 is equal to V_μ ; and

calculating on the grid the probability that the company will have a value of v_m at time t_n by the vector $P_n = (p_{0,n}, \dots, p_{m,n}, \dots, p_{M,n})$ where initial vector $P_0 = (0, \dots, 1/h_\mu, \dots, 0)$.,

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14. A method in accordance with claim 13 wherein the step of determining the transitional probability that the company will have a value of v_m at time t_n comprises the steps of:

determining the unconditional probability vector \bar{P}_1 in accordance with the formula

$$\bar{P}_1 = \hat{T}_{0,1} P_0$$

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wherein $\hat{T}_{0,1}$ is the transition operator between the times t_0 and t_1 for the equation

$$\frac{dV}{V} = (r - \lambda\kappa)dt + \sigma dW + (e^J - 1)dN$$

wherein like variables to those defined above define the same values and wherein; and

applying a projection operator $\hat{\Pi}_1$ to vector \bar{P}_1 in order to obtain the vector P_1 :

$$P_1 = \hat{\Pi}_1 \bar{P}_1.$$

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15. A method in accordance with claim 14 and further comprising the step of determining selected financial characteristics of the company as a function of the at least one probability vector P .

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16. A method in accordance with claim 15 and further comprising the step of calculating the survival probability of the company in accordance with the equation

$$Q_n = \sum_{m=0}^M P_{m,n}$$

where

m is an index changing from 0 to M ,

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M is the total number of grid points,

n is an index changing from 0 to N , and

N is the total number of times when company value is observed.

17. A method in accordance with claim 15 and further comprising the step of calculating the equity value of the company in accordance with the equation

$$S = e^{-rT} \sum_{m=0}^M P_{m,N} \max(v_m - B_N, 0).$$

where

5 r is the interest rate,

T is the maturity of debt,

m is an index changing from 0 to M ,

v_m represents the value of the company,

N is the total number of times when company value is observed,

10 M is the total number of grid points, and

B_N is the terminal debt level.

18. A method in accordance with claim 15 and further comprising the step of calculating the present value of company debt δ in accordance with the equation

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$$\delta = e^{-rT} \sum_{m=0}^M P_{m,N}$$

where

r is the interest rate,

T is the maturity of debt,

N is the total number of times when company value is observed,

20 m is an index changing from 0 to M , and

M is the total number of grid points.

19. A method in accordance with claim 16 and further comprising the step of calculating the credit default spread CDS in accordance with the equation

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$$CDS_n = (1 - R) \left(\frac{1 - e^{-r_n} Q_n}{\frac{1}{2} e^{-r_0} (t_1 - t_0) + \frac{1}{2} \sum_{n'=1}^{n-1} e^{-r_{n'}} (t_{n'+1} - t_{n'-1}) + \frac{1}{2} e^{-r_n} (t_n - t_{n-1})} - r \right)$$

where

r is the interest rate,

t_n is the observational time between today and maturity T ,

R is a recovery level for a selected debt seniority,

n is an index changing from 1 to N , and

n' is an index changing from 1 to $n-1$.

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20. A method in accordance with claim 15 wherein the step of determining the value of a vector P_n is performed with the transition operators $\hat{T}_{0,1}$ being a Toeplitz matrix.

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21. A method in accordance with claim 20 wherein the step of determining the value of a vector P_n is performed using a Fast Fourier Transform.

22. A system for calculating the financial status of a company, comprising:

a processor;

a memory connected to the processor and storing instructions for controlling the operation

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of the processor;

the processor operative with the instructions in the memory to perform the steps of

determining the company's value in accordance with the formula

$$\frac{dV}{V} = (r - \lambda\kappa)dt + \sigma dW + (e^J - 1)dN$$

wherein

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N is the standard Poisson process with intensity λ ,

J is a normal variable with mean j and standard deviation k ;

W is the standard Wiener process,

V is the value of the company,

r is the risk neutral rate of the company,

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σ is the company volatility,

λ is the intensity of the jump arrival,

t is calendar time between today and maturity T ; and

determining that the company defaults if at a sequence of discrete observational times

$t_0 = 0(\text{today}), t_1, t_2, \dots, t_N = T(\text{maturity})$ the value of the company $V_n = V(t_n)$ falls below a

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corresponding barrier level $B_1, B_2, \dots, B_N = D$, the barrier levels selected to represent different debt amounts which come due at corresponding times $t_0 = 0(\text{today}), t_1, t_2, \dots, t_N = T(\text{maturity})$.

23. The system of claim 22 and further comprising calculating the transitional probability density function (*TPDF*) for the value of the company conditional on no default occurring between time $t = 0$ and an observational time t_x comprising the steps of:

5 selecting a range for the natural logarithm of the value of the company $U = \ln(V)$:

$$U_{\min} < U < U_{\max}$$

where

$$U_{\min} = -nsd \div \sqrt{(\sigma^2 + k^2)} T + \min(r - \lambda \kappa - \sigma^2 / 2, 0) T$$

and

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$$U_{\max} = nsd \div \sqrt{(\sigma^2 + k^2)} T + \max(r - \lambda \kappa - \sigma^2 / 2, 0) T$$

and where *nsd* is the number of standard deviations used to characterize the extreme values of the natural logarithm of the value of the company;

dividing the range into an equidistant grid $u_0 = U_{\min}, u_1, \dots, u_m, \dots, u_M = U_{\max}$ of *M* steps,

15 with each grid step, denoted by *h*, equal to $h = (U_{\max} - U_{\min}) / M$, with the total number of points in the grid, which is equal to *M*+1, being a power of 2;

defining the integer $\mu = \text{floor}(-U_{\min} / h)$, where *floor*(.) is a mathematical function, which for every number defines an integer less than or equal to this number;

constructing the modified grid as: $\tilde{u}_m = (m - \mu)h$, $m = 0, 1, \dots, M$. ;

20 defining a grid on the line representing the value of the company using the following formula

$$v_m = V_0 \exp(u_m) \quad m = 0, 1, \dots, M$$

where the initial value of the company V_0 is equal to V_μ ; and

calculating on the grid the probability that the company will have a value of v_m at time t_n

25 by the vector $P_n = (p_{0,n}, \dots, p_{m,n}, \dots, p_{M,n})$ where initial vector $P_0 = (0, \dots, 1/h_\mu, \dots, 0)$.,

24. The system of claim 23 wherein the step of determining the transitional probability that the company will have a value of v_m at time t_n comprises the steps of:

determining the unconditional probability vector \bar{P}_1 in accordance with the formula

$$\bar{P}_1 = \hat{T}_{0,1} P_0$$

wherein $\hat{T}_{0,1}$ is the transition operator between the times t_0 and t_1 for the equation

$$\frac{dV}{V} = (r - \lambda\kappa)dt + \sigma dW + (e^J - 1)dN$$

wherein like variables to those defined above define the same values and wherein; and

5 applying a projection operator $\hat{\Pi}_1$ to vector \bar{P}_1 in order to obtain the vector P_1 :

$$P_1 = \hat{\Pi}_1 \bar{P}_1.$$

25. The system of claim 24 and further comprising the step of determining selected financial characteristics of the company as a function of the at least one probability vector P .

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26. The system of claim 25 and further comprising the step of calculating the survival probability of the company in accordance with the equation

$$Q_n = \sum_{m=0}^M P_{m,n}$$

where

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m is an index changing from 0 to M ,

M is the total number of grid points,

n is an index changing from 0 to N , and

N is the total number of times when company value is observed.

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27. The system of claim 25 and further comprising the step of calculating the equity value of the company in accordance with the equation

$$S = e^{-rT} \sum_{m=0}^M P_{m,N} \max(v_m - B_N, 0).$$

where

r is the interest rate,

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T is the maturity of debt,

m is an index changing from 0 to M ,

v_m represents the value of the company,

N is the total number of times when company value is observed,

M is the total number of grid points, and
 B_N is the terminal debt level.

28. The system of claim 25 and further comprising the step of calculating the present value of
 5 company debt δ in accordance with the equation

$$\delta = e^{-rT} \sum_{m=0}^M P_{m,N}$$

where

r is the interest rate,

T is the maturity of debt,

10 N is the total number of times when company value is observed,

m is an index changing from 0 to M , and

M is the total number of grid points.

29. The system of claim 26 and further comprising the step of calculating the credit default
 15 spread CDS in accordance with the equation

$$CDS_n = (1 - R) \left(\frac{1 - e^{-r_n} Q_n}{\frac{1}{2} e^{-r_0} (t_1 - t_0) + \frac{1}{2} \sum_{n'=1}^{n-1} e^{-r_{n'}} (t_{n'+1} - t_{n'-1}) + \frac{1}{2} e^{-r_n} (t_n - t_{n-1})} - r \right)$$

where

r is the interest rate,

20 t_n is the observational time between today and maturity T ,

R is a recovery level for a selected debt seniority,

n is an index changing from 1 to N , and

n' is an index changing from 1 to $n-1$.

25 30. The system of claim 25 wherein the step of determining the value of a vector P_n is
 performed with the transition operators $\hat{T}_{0,1}$ being a Toeplitz matrix.

31. The system of claim 30 wherein the step of determining the value of a vector P_n is
 performed using a Fast Fourier Transform.

32. A system for calculating the financial status of a company, comprising:
means for determining the company's value in accordance with the formula

$$\frac{dV}{V} = (r - \lambda\kappa)dt + \sigma dW + (e^J - 1)dN$$

wherein

N is the standard Poisson process with intensity λ ,

J is a normal variable with mean j and standard deviation k ;

W is the standard Wiener process,

V is the value of the company,

r is the risk neutral rate of the company,

σ is the company volatility,

λ is the intensity of the jump arrival,

t is calendar time between today and maturity T ; and

means for determining that the company defaults if at a sequence of discrete observational times $t_0 = 0(\text{today}), t_1, t_2, \dots, t_N = T(\text{maturity})$ the value of the company $V_n = V(t_n)$ falls below a corresponding barrier level $B_1, B_2, \dots, B_N = D$, the barrier levels selected to represent different debt amounts which come due at corresponding times $t_0 = 0(\text{today}), t_1, t_2, \dots, t_N = T(\text{maturity})$.

33. A method operable on a computer for calculating the financial status of a company, comprising the steps of:

calculating the value over time of a company in accordance with Zhou's model;

determining that the company defaults if at a sequence of discrete observational times the value of the company falls below a corresponding barrier level;

the barrier levels selected to represent different debt amounts which come due at corresponding times; and

calculating the transitional probability density function for the value of the company conditional on no default occurring between an initial time and an observational time using a probability vector P .

34. A method in accordance with claim 33 wherein the probability vector P is determined using a projection operator nullifying the components of the probability vector below the barrier and further comprising the step of determining selected financial characteristics of the company as a function of the probability vector P .

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35. A method in accordance with claim 34 wherein the financial characteristic is selected from the group comprising the equity value of a company, the debt value of a company, the survival probability of a company and the value of the credit default spread.

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36. The method of claim 34 wherein the step of determining the value of the probability vector P is performed with a transition operators $\hat{T}_{0,1}$ being a Toeplitz matrix.

37. The method of claim 36 wherein the step of determining the value of the probability vector P is performed using a Fast Fourier Transform.

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38. A system for calculating the financial status of a company, comprising the steps of:
a processor;

a memory connected to the processor and storing instructions to control the operation of the processor to perform the steps of

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calculating the value over time of a company in accordance with Zhou's model;
determining that the company defaults if at a sequence of discrete observational times the value of the company falls below a corresponding barrier level;

the barrier levels selected to represent different debt amounts which come due at corresponding times; and

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calculating the transitional probability density function for the value of the company conditional on no default occurring between an initial time and an observational time using a probability vector P .

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39. A system in accordance with claim 38 wherein the probability vector P is determined using a projection operator nullifying the components of the probability vector below the barrier and further comprising the step of determining selected financial characteristics of the company as a function of the probability vector P .

40. A system in accordance with claim 39 wherein the financial characteristic is selected from the group comprising the equity value of a company, the debt value of a company, the survival probability of a company and the value of the credit default spread.

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41. a system in accordance with claim 40 wherein the step of determining the value of the probability vector P is performed with a transition operators $\hat{T}_{0,1}$ being a Toeplitz matrix.

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42. A system in accordance with claim 41 wherein the step of determining the value of the probability vector P is performed using a Fast Fourier Transform.

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43. A system for calculating the financial status of a company, comprising:

means for calculating the value over time of a company in accordance with Zhou's model;

means for determining that the company defaults if at a sequence of discrete observational times the value of the company falls below a corresponding barrier level;

the barrier levels selected to represent different debt amounts which come due at corresponding times; and

means for calculating the transitional probability density function for the value of the company conditional on no default occurring between an initial time and an observational time using a probability vector P .

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44. A program product operable on a computer to control the operation of the computer to calculate the financial status of a company, the program product comprising a computer-readable medium storing instructions to perform the steps of:

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calculating the value over time of a company in accordance with Zhou's model;

determining that the company defaults if at a sequence of discrete observational times the value of the company falls below a corresponding barrier level;

the barrier levels selected to represent different debt amounts which come due at corresponding times; and

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calculating the transitional probability density function for the value of the company conditional on no default occurring between an initial time and an observational time using a probability vector P .